

# Observables and Brackets in the Hamiltonian formulation of physical theories

List of selected references, related to the talk given at Universidad de los Andes, the 03th of August 2015 (given by Dimitri VEY <sup>1</sup>)

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